

Modelling Light Transmission in a Fiber-Optical Reflection System

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Received: 26.11.2003

Accepted: 19.01.2004

Abstract. Light transmission in the reflection fiber system, located in external optical media, has been investigated for application as sensors. The system was simulated by different models, including external cavity parameters such as the distance between light emitting and receiving fibers and mirror positioning distance. The sensitivity to a linear displacement of the sensors was studied as a function of the distance between the tips of the light emitting fiber and the center of the pair reflected light collecting fibers, by positioning a mirror. Physical fundamentals and operating principles of the advanced fiber optical sensors were revealed.

Keywords: fiber-optical sensor, displacement sensor, refractometer.

1 Introduction

Investigation of the reflection fiber system arrangement and influence of physical and optical parameters of a cavity on light transmission promises the creation of a lot of devices for measuring physical properties of the external optical media and cavity dimension changes.

In recent years W.H.Ko et al [1] have proposed a new innovative, external influence compensated method – a fiber optical reflective displacement micrometer, which consisted of the light transmitting fiber and a pair of light

receiving fibers on a plane. The tips of the pair of the receiving fibers detect the light reflected from a mirror and form an angle with the light emitting fiber. The experimental dependence of the output signal of the micrometer after fixing not commented parameters of the fibers and construction of the micrometer have been obtained.

The aim of this paper is to investigate the influence of the arrangement of the reflection fiber system on light transmission: (i) the influence of physical properties of a cavity, (ii), to show the sensitivity of the fiber optical system dependence on the fiber tips distribution distance b_1 . We demonstrate a possibility: (i) to use fibers with a defined angle between the tips of fibers at the mirror in a measuring head and the same light source as a sensor for increased sensitivity measuring of the linear displacement, (ii) to show that the light source degradation and temperature fluctuations can be compensated.

2 Principle of operation (main equations)

The arrangement of the fiber tips in Fig. 1 was applied to explain the main physical principle of operation of the reflection fiber system. If the reflecting surface is a perfect mirror, the reflected light is equivalent to that transmitted with the source L , at the mirrored position L' a distance z away. According to [2], the intensity distribution function of the source $I(r, z)$ at the position $Q(r, z)$ on the plane $z(h)$ away from the source and r away from the light beam axis is [2]

$$I(r, z) = I_0 K_0 \frac{\exp \{r^2/R^2(z)\}}{R^2(z)}. \quad (1)$$

I_0 is the intensity of the light source, K_0 is the loss of the intensity of the input fiber; $n = 1$. $R(z)$ is the effective radius of the output optical field, defined as

$$R(z) = a_0 + kz \tan(\theta_c), \quad (2)$$

$2a_0$ is the radius of the fiber core, θ_c is the aperture angle of the fiber, k is a constant of the light source. Contrary to [1, 2], we consider $R(z)$ to be a linear function, because of the well-known linear spreading of light.

If the reflecting surface is not perfect and has the reflection coefficient R_M , the reflected light will be reduced by the factor r .

(Fig. 1):

$$A = I_A = S_1 \frac{K_0 R_M K_1 I_0 \exp \{ - (x + d)^2 / R^2(z) \}}{\pi R^2(z)}, \quad (4)$$

$$B = I_B = S_2 \frac{K_0 R_M K_2 I_0 \exp \{ - (x - d)^2 / R^2(z) \}}{\pi R^2(z)}, \quad (5)$$

where $2d$ is the distance between the centers of the light receiving fibers, $2a$ is the diameter of the fiber with cladding. In particular case $2d$ can be equal to $2a$.

When the two receiving fibers are identical, $K_1 = K_2$, $S_1 = S_2$ and

$$\frac{(A - B)}{(A + B)} = \frac{\exp \{ - (x + d)^2 / R^2(z) \} - \exp \{ - (x - d)^2 / R^2(z) \}}{\exp \{ - (x + d)^2 / R^2(z) \} + \exp \{ - (x - d)^2 / R^2(z) \}}. \quad (6)$$

According to Fig. 1, $X = x = 2h' \sin \theta$. Equation (6) is a function not only of x , but also of z .

$$z = (z_0 \pm \Delta z)n, \quad (7)$$

where

$$z_0 = \frac{b_1}{\sin \theta}, \quad \Delta z = \frac{2h'}{\cos \theta}.$$

Then

$$z = \left(\frac{b_1}{\sin \theta} \pm \frac{2h'}{\cos \theta} \right) n. \quad (8)$$

Here z_0 and h_0 are the initial reference values when $A = B$, ($U_A = U_B$), $U_A - U_B = 0$ is the crossover point of the signals $A(h)$, and $B(h)$ is the main principle of the system operation. Refractive index $n = 1$.

$$h = h_0 \pm h'. \quad (9)$$

Function (6) can be expressed only as a function h , n , θ , θ_c , b_1 (Fig. 1). $(A - B)/(A + B)$ does not depend on S_1 , K_1 , R_M , K_0 , I_0 , in contrast to $(A - B)$ that depends on them.

The compensation mechanism, signal $(A - B)/(A + B)$, does not depend on the reflection coefficient of mirror, intensity of the light source, and loss in the fibers. Equations (4), (5) and (6) were used as functions h for simulating the output signals U_{out} of sensors in order to compare the sensitivity $S = dU_{out}/dh$ of our fiber sensor constructions with those known in literature.

3 Results

The signal characteristics of the system are

$$A(h), B(h), C(h) = A(h) - B(h), \quad V(h) = C(h)/[A(h) + B(h)],$$

$$S_A = G(h) = \frac{dA}{dh}, \quad S_B = F(h) = \frac{dB}{dh}, \quad S_{sub} = \frac{dC}{dh}, \quad S_{div} = \frac{dV}{dh}.$$

For calculating applied such parameter b_1 values 1, 2, 3, 4 mm. The last value is as in [3] for comparison of the S_{sub} and S_{div} results. The diameter of the fiber core is $a_0 = 0.2$ mm, with cladding $a = 0.4$ mm, the fiber aperture angle $\theta_c = 19.5^\circ$ and the angle $\theta = 25^\circ$. The distance between fibers A and B is $d = 0.3$ mm. The output signal for all pictures is in the same arbitrary units.

The output signals $A(h)$ and $B(h)$ in Fig. 2 rise from zero to the maximum value and then drop off. The portion in affinity of the points A_1, A_2 and B_1, B_2 ,

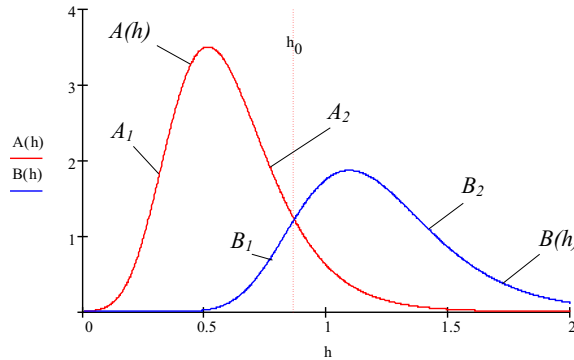


Fig. 2. Dependence of signals A and B on the mirror position h . $\theta = 30^\circ$, $b_1 = 1$ mm.

B_2 for these characteristics is linear. The maximum amplitude A_{max} of signal $A(h)$ is always higher than B_{max} for signal $B(h)$. Sensitivity $G(h)$ and $F(h)$ (Fig. 3) on the near side of this characteristics is higher than that as in the far side. Moreover the sensitivity of the curve $B(h)$ is lower than that of $A(h)$ on both sides. The characteristics $A(h)$ and $B(h)$ naturally cross each other at an appropriate value of h_0 .

The calculation results of the characteristics $A(h)$ and $B(h)$ with different values of the system parameter b_1 are represented in Fig. 4.

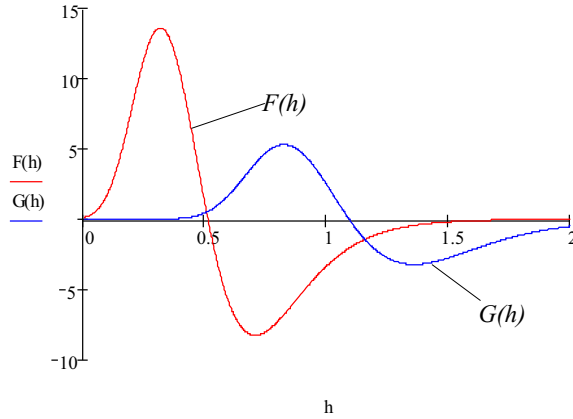


Fig. 3. Sensitivity dependence to the signals A and B on the mirror position h : $G(h) = d[A(h)]/dh$, $F(h) = d[B(h)]/dh$.

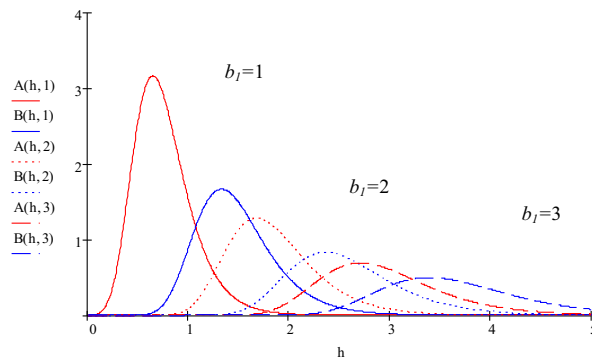


Fig. 4. Dependence of signals A and B on the mirror position h as $b_1 = 1, 2, 3$ mm.

The maximum values of the characteristics $A(h)$ and $B(h)$ decrease as b_1 increases. The maximum points of all characteristics and their crossing points are at the higher values of h with increasing b_1 . As theoretical equations (4) and (5) show the decrease of A_{max} , B_{max} will be exponential.

The characteristics $C(h) = A(h) - B(h)$ Fig. 5 rise from zero to the positive maximum value, then drop to zero, and rise to the negative maximum value and afterwards decrease to zero. For application in practical measurements, the linear part of the characteristic at the value $h = h_0$ is more important. Measuring values $C(h)$ everyone can determine the value of the mirror or body

displacement from position $h_0 \pm h'$. The amplitude of signal $C(h)$ decreases as b_1 increases, the distance h_0 increases as well. The characteristics $S_{sub}(h)$ in Fig. 6 reveal the sensitivity to displacement to be very low as $b_1 = 4$ mm.

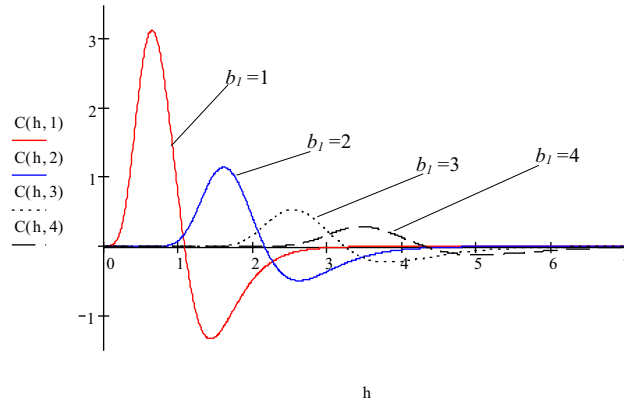


Fig. 5. Dependence of signals $C(h) = A(h) - B(h)$ on the mirror position h as $b_1 = 1, 2, 3, 4$ mm.

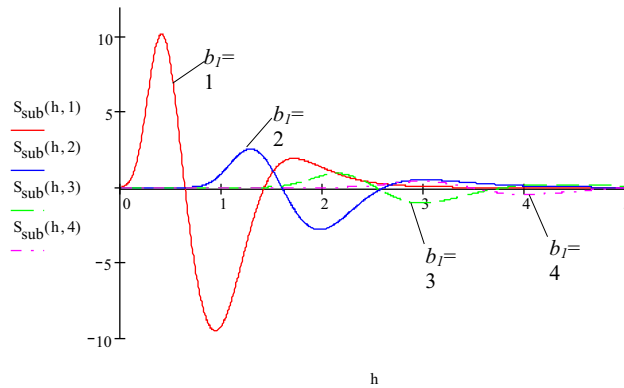


Fig. 6. Dependence of signals $S_{sub}(h)$ on the mirror position h as $b_1 = 1, 2, 3, 4$ mm.

This is the main reason why the values of $S_{sub}(h)$ are so low as the distance b_1 is not properly chosen for the system. Moreover, the greater the signal $C(h)$ the better the resolution of the system is.

Very important for compensated measurements is system signal (Fig. 7)

$$V = (A - B)/(A + B).$$

This figure shows the signal to be ± 1 and zero at definite $h = h_0$ values.

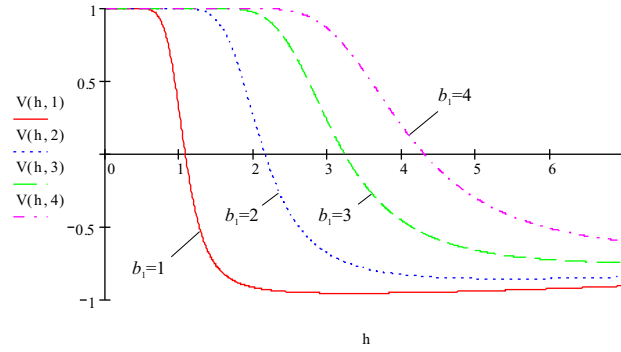


Fig. 7. Dependence of signals $V(h) = A(h) - B(h)/A(h) + B(h)$ on the mirror position h as $b_1 = 1, 2, 3, 4$ mm.

Those values of h increase as b_1 increase. The characteristics $V(h)$ have linear parts in the affinity of zero. Therefore each of them is proper for measurement not only the mirror displacement h' , but also its direction. S_{div} decreases exponentially as b_1 increases (Fig. 8).

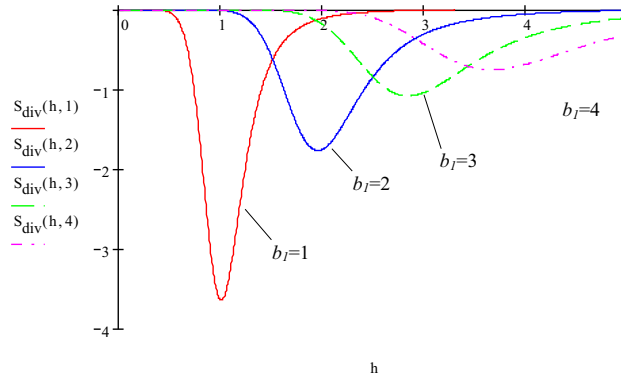


Fig. 8. Dependence of signals $S_{div}(h)$ on the mirror position h as $b_1 = 1, 2, 3, 4$ mm.

4 Conclusion

Light transmission modelling in the reflection fiber-optical system revealed that the sensitivity could increase as the parameter of the system b_1 is de-

creased as much as possible. All the modelling results are coincidental with the experimental data [3].

References

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